

《物理学和工程学中的数学方法》

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内容概要

Since the publication of the first edition of this book, both through teaching the material it covers and as a result of receiving helpful comments from colleagues, we have become aware of the desirability of changes in a number of areas. The most important of these is that the mathematical preparation of current senior college and university entrants is now less thorough than it used to be. To match this, we decided to include a preliminary chapter covering areas such as polynomial equations, trigonometric identities, coordinate geometry, partial fractions, binomial expansions, necessary and sufficient condition and proof by induction and contradiction.

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作者简介

KEN RILEY read Mathematics at the University of Cambridge and proceeded to a Ph.D. there in theoretical and experimental nuclear physics. He became a Research Associate in elementary particle physics at Brookhaven, and then, having taken up a lectureship at

书籍目录

- preface to the second edition
- preface to the first edition
- 1 preliminary algebra
 - 1.1 simple functions and equations
 - polynomial equations; factorisation; properties of roots
 - 1.2 trigonometric identities
 - single angle; compound-angles; double- and half-angle identities
 - 1.3 coordinate geometry
 - 1.4 partial fractions
 - complications and special cases
 - 1.5 binomial expansion
 - 1.6 properties of binomial coefficients
 - 1.7 some particular methods of proof
 - proof by induction; proof by contradiction; necessary and sufficient conditions
 - 1.8 exercises
 - 1.9 hints and answers
- 2 preliminary calculus
 - 2.1 differentiation
 - differentiation from first principles: products; the chain rule; quotients; implicit differentiation; logarithmic differentiation; leibnitz' theorem; special points of a function: curvature: theorems of differentiation
 - 2.2 integration
 - .integration from first principles; the inverse of differentiation; by inspection; sinusoidal jhnctions; logarithmic integration; using partial fractions;substitution method; integration by parts; reduction formulae; infinite and improper integrals; plane polar coordinates; integral inequalities; applications of integration
 - 2.3 exercises
 - 2.4 hints and answers
- 3 complex numbers and hyperbolic functions
 - 3.1 the need for complex numbers
 - 3.2 manipulation of complex numbers
 - addition and subtraction; modulus and argument; multiplication; complex conjugate; division
 - 3.3 polar representation of complex numbers multiplication and division in polar form
 - 3.4 de moivre's theorem
 - trigonometric identities;finding the nth roots of unity: solving polynomial equations
 - 3.5 complex logarithms and complex powers
 - 3.6 applications to differentiation and integration
 - 3.7 hyperbolic functions
 - definitions; hyperbolic-trigonometric analogies; identities of hyperbolic functions: solving hyperbolic equations; inverses of hyperbolic functions;calculus of hyperbolic functions
 - 3.8 exercises
 - 3.9 hints and answers
- 4 series and limits
 - 4.1 series
 - 4.2 summation of series
 - arithmetic series; geometric series; arithmetico-geometric series; the difference method; series involving natural numbers; transformation of series
 - 4.3 convergence of infinite series
 - absolute and conditional convergence; series containing only real positive terms; alternating series test

4.4 operations with series

4.5 power series

convergence of power series; operations with power series

4.6 taylor series

taylor's theorem; approximation errors; standard maclaurin series

4.7 evaluation of limits

4.8 exercises

4.9 hints and answers

5 partial differentiation

5.1 definition of the partial derivative

5.2 the total differential and total derivative

5.3 exact and inexact differentials

5.4 useful theorems of partial differentiation

5.5 the chain rule

5.6 change of variables

5.7 taylor's theorem for many-variable functions

5.8 stationary values of many-variable functions

5.9 stationary values under constraints

5.10 envelopes

5.11 thermodynamic relations

5.12 differentiation of integrals

5.13 exercises

5.14 hints and answers

6 multiple integrals

6.1 double integrals

6.2 triple integrals

6.3 applications of multiple integrals

areas and volumes; masses, centres of mass and centroids; pappus' theorems; moments of inertia; mean values of functions

6.4 change of variables in multiple integrals

change of variables in double integrals; evaluation of the integral i = change of variables in triple integrals; general properties of jacobians

6.5 exercises

6.6 hints and answers

7 vector algebra

7.1 scalars and vectors

7.2 addition and subtraction of vectors

7.3 multiplication by a scalar

7.4 basis vectors and components

7.5 magnitude of a vector

7.6 multiplication of vectors

scalar product; vector product; scalar triple product; vector triple product

7.7 equations of lines, planes and spheres

7.8 using vectors to find distances

point to line; point to plane; line to line; line to plane

7.9 reciprocal vectors

7.10 exercises

7.11 hints and answers

8 matrices and vector spaces

8.1 vector spaces

basis vectors; inner product; some useful inequalities

8.2 linear operators

8.3 matrices

8.4 basic matrix algebra

matrix addition; multiplication by a scalar; matrix multiplication

8.5 functions of matrices

8.6 the transpose of a matrix

8.7 the complex and hermitian conjugates of a matrix

8.8 the trace of a matrix

8.9 the determinant of a matrix

properties of determinants

8.10 the inverse of a matrix

8.11 the rank of a matrix

8.12 special types of square matrix

diagonal; triangular; symmetric and antisymmetric ; orthogonal; hermitian and anti-hermitian; unitary; normal

8.13 eigenvectors and eigenvalues

of a normal matrix; of hermitian and anti-hermitian matrices; of a unitary matrix; of a general square matrix

8.14 determination of eigenvalues and eigenvectors

degenerate eigenvalues

8.15 change of basis and similarity transformations

8.16 diagonalisation of matrices

8.17 quadratic and hermitian forms

stationary properties of the eigenvectors ; quadratic surfaces

8.18 simultaneous linear equations

range; null space; n simultaneous linear equations in n unknowns; singular value decomposition

8.19 exercises

8.20 hints and answers

9 normal modes

9.1 typical oscillatory systems

9.2 symmetry and normal modes

9.3 rayleigh-ritz method

9.4 exercises

9.5 hints and answers

10 vector calculus

10.1 differentiation of vectors

composite vector expressions; differential of a vector

10.2 integration of vectors

10.3 space curves

10.4 vector functions of several arguments

10.5 surfaces

10.6 scalar and vector fields

10.7 vector operators

gradient of a scalar field: divergence of a vector field: curl of a vector field

10.8 vector operator formulae

vector operators acting on sums and products; combinations of grad, div and curl

10.9 cylindrical and spherical polar coordinates

10.10 general curvilinear coordinates

10.11 exercises

10.12 hints and answers

11 line, surface and volume integrals

11.1 line integrals

evaluating line integrals; physical examples; line integrals with respect to a scalar

11.2 connectivity of regions

11.3 green's theorem in a plane

11.4 conservative fields and potentials

11.5 surface integrals

evaluating surface integrals; vector areas of surfaces; physical examples

11.6 volume integrals

volumes of three-dimensional regions

11.7 integral forms for grad, div and curl

11.8 divergence theorem and related theorems

green's theorems; other related integral theorems; physical applications

11.9 stokes' theorem and related theorems

related integral theorems: physical applications

11.10 exercises

11.11 hints and answers

12 fourier series

12.1 the dirichlet conditions

12.2 the fourier coefficients

12.3 symmetry considerations

12.4 discontinuous functions

12.5 non-periodic functions

12.6 integration and differentiation

12.7 complex fourier series

12.8 parseval's theorem

12.9 exercises

12.10 hints and answers

13 integral transforms

13.1 fourier transforms

the uncertainty principle; fraunhofer diffraction: the dirac δ -function: relation of the δ -function to fourier

transforms; properties of fourier transforms; odd and even functions; convolution and deconvolution; correlation

functions and energy spectra; parseval's theorem; fourier transforms in higher dimensions

13.2 laplace transforms

laplace transforms of derivatives and integrals; other properties of laplace transforms

13.3 concluding remarks

13.4 exercises

13.5 hints and answers

14 first-order ordinary differential equations

14.1 general form of solution

14.2 first-degree first-order equations

separable-variable equations; exact equations; inexact equations, integrating factors; linear equations;

homogeneous equations; isobaric equations: bernoulli's equation; miscellaneous equations

14.3 higher-degree first-order equations

equations soluble for p ; for x ; for y ; clairaut's equation

14.4 exercises

14.5 hints and answers

15 higher-order ordinary differential equations

15.1 linear equations with constant coefficients

finding the complementary function $y_c(x)$; finding the particular integral $y_p(x)$; constructing the general solution $y_c(x) + y_p(x)$; linear recurrence relations: laplace transform method

15.2 linear equations with variable coefficients

the legendre and euler linear equations; exact equations; partially known complementary function; variation of parameters; green's functions; canonical form for second-order equations

15.3 general ordinary differential equations

dependent variable absent; independent variable absent; non-linear exact equations; isobaric or homogeneous equations; equations homogeneous in x or y alone; equations having $y = aex$ as a solution

15.4 exercises

15.5 hints and answers

16 series solutions of ordinary differential equations

16.1 second-order linear ordinary differential equations

ordinary and singular points

16.2 series solutions about an ordinary point

16.3 series solutions about a regular singular point

distinct roots not differing by an integer; repeated root of the indicial equation; distinct roots differing by an integer

16.4 obtaining a second solution

the wronskian method; the derivative method; series form of the second solution

16.5 polynomial solutions

16.6 legendre's equation

general solution for integer l ; properties of legendre polynomials

16.7 bessers equation

general solution for non-integer ν ; general solution for integer ν ; properties of bessel functions

16.8 general remarks

16.9 exercises

16.10 hints and answers

17 eigenfunction methods for differential equations

17.1 sets of functions

some useful inequalities

17.2 adjoint and hermitian operators

17.3 the properties of hermitian operators

reality of the eigenvalues; orthogonality of the eigenfunctions; construction of real eigenfunctions

17.4 sturm-liouville equations

valid boundary conditions; putting an equation into sturm-liouville form

17.5 examples of sturm-liouville equations

legendre's equation; the associated legendre equation; bessel's equation; the simple harmonic equation; hermite's equation; laguerre's equation; chebyshev's equation

17.6 superposition of eigenfunctions: green's functions

17.7 a useful generalisation

17.8 exercises

17.9 hints and answers

18 partial differential equations: general and particular solutions

18.1 important partial differential equations

the wave equation; the diffusion equation; laplace's equation; poisson's equation; schrodinger's equation

18.2 general form of solution

18.3 general and particular solutions

first-order equations; inhomogeneous equations and problems; second-order equations

18.4 the wave equation

- 18.5 the diffusion equation
- 18.6 characteristics and the existence of solutions
- first-order equations; second-order equations
- 18.7 uniqueness of solutions
- 18.8 exercises
- 18.9 hints and answers
- 19 partial differential equations: separation of variables and other methods
- 19.1 separation of variables: the general method
- 19.2 superposition of separated solutions
- 19.3 separation of variables in polar coordinates
- laplace's equation in polar coordinates: spherical harmonics: other equations in polar coordinates; solution by expansion; separation of variables for inhomogeneous equations
- 19.4 integral transform methods
- 19.5 inhomogeneous problems-green's functions
- similarities to green's functions for ordinary differential equations: general boundary-value problems: dirichlet problems; neumann problems
- 19.6 exercises
- 19.7 hints and answers
- 20 complex variables
- 20.1 functions of a complex variable
- 20.2 the cauchy-riemann relations
- 20.3 power series in a complex variable
- 20.4 some elementary functions
- 20.5 multivalued functions and branch cuts
- 20.6 singularities and zeroes of complex functions
- 20.7 complex potentials
- 20.8 conformal transformations
- 20.9 applications of conformal transformations
- 20.10 complex integrals
- 20.11 cauchy's theorem
- 20.12 cauchy's integral formula
- 20.13 taylor and laurent series
- 20.14 residue theorem
- 20.15 location of zeroes
- 20.16 integrals of sinusoidal functions
- 20.17 some infinite integrals
- 20.18 integrals of multivalued functions
- 20.19 summation of series
- 20.20 inverse laplace transform
- 20.21 exercises
- 20.22 hints and answers
- 21 tensors
- 21.1 some notation
- 21.2 change of basis
- 21.3 cartesian tensors
- 21.4 first- and zero-order cartesian tensors
- 21.5 second- and higher-order cartesian tensors
- 21.6 the algebra of tensors
- 21.7 the quotient law

- 21.8 the tensors and
- 21.9 isotropic tensors
- 21.10 improper rotations and pseudotensors
- 21.11 dual tensors
- 21.12 physical applications of tensors
- 21.13 integral theorems for tensors
- 21.14 non-cartesian coordinates
- 21.15 the metric tensor
- 21.16 general coordinate transformations and tensors
- 21.17 relative tensors
- 21.18 derivatives of basis vectors and christoffel symbols
- 21.19 covariant differentiation
- 21.20 vector operators in tensor form
- 21.21 absolute derivatives along curves
- 21.22 geodesics
- 21.23 exercises
- 21.24 hints and answers
- 22 calculus of variations
- 22.1 the euler-lagrange equation
- 22.2 special cases
- f does not contain y explicitly; f does not contain x explicitly
- 22.3 some extensions
- several dependent variables; several independent variables; higher-order derivatives: variable end-points
- 22.4 constrained variation
- 22.5 physical variational principles
- fermat's principle in optics; hamilton's principle in mechanics
- 22.6 general eigenvalue problems
- 22.7 estimation of eigenvalues and eigenfunctions
- 22.8 adjustment of parameters
- 22.9 exercises
- 22.10 hints and answers
- 23 integral equations
- 23.1 obtaining an integral equation from a differential equation
- 23.2 types of integral equation
- 23.3 operator notation and the existence of solutions
- 23.4 closed-form solutions
- separable kernels; integral transform methods; differentiation
- 23.5 neumann series
- 23.6 fredholm theory
- 23.7 schmidt-hilbert theory
- 23.8 exercises
- 23.9 hints and answers
- 24 group theory
- 24.1 groups
- definition of a group; examples of groups
- 24.2 finite groups
- 24.3 non-abelian groups
- 24.4 permutation groups
- 24.5 mappings between groups

24.6 subgroups

24.7 subdividing a group

equivalence relations and classes; congruence and cosets; conjugates and classes

24.8 exercises

24.9 hints and answers

25 representation theory

25.1 dipole moments of molecules

25.2 choosing an appropriate formalism

25.3 equivalent representations

25.4 reducibility of a representation

25.5 the orthogonality theorem for irreducible representations

25.6 characters

orthogonality property of characters

25.7 counting irreps using characters

summation rules for irreps

25.8 construction of a character table

25.9 group nomenclature

25.10 product representations

25.11 physical applications of group theory

bonding in molecules: matrix elements in quantum mechanics: degeneracy of normal modes: breaking of degeneracies

25.12 exercises

25.13 hints and answers

26 probability

26.1 venn diagrams

26.2 probability

axioms and theorems; conditional probability; bayes' theorem

26.3 permutations and combinations

26.4 random variables and distributions

discrete random variables; continuous random variables

26.5 properties of distributions

mean: mode and median: variance and standard deviation: moments:

central moments

26.6 functions of random variables

26.7 generating functions

probability generating functions; moment generating functions; characteristic functions; cumulant generating functions

26.8 important discrete distributions

binomial; geometric; negative binomial; hypergeometric ; poisson

26.9 important continuous distributions

gaussian : log-normal; exponential; gamma; chi-squared; cauchy ; breitwigner : uniform

26.10 the central limit theorem

26.11 joint distributions

discrete bivariate ; continuous bivariate ; marginal and conditional distributions

26.12 properties of joint distributions

means; variances; covariance and correlation

26.13 generating functions for joint distributions

26.14 transformation of variables in joint distributions

26.15 important joint distributions

multinomial multivariate gaussian

26.16 exercises

26.17 hints and answers

27 statistics

27.1 experiments, samples and populations

27.2 sample statistics

averages; variance and standard deviation; moments; covariance and correlation

27.3 estimators and sampling distributions

consistency, bias and efficiency; fisher's inequality; standard errors; confidence limits

27.4 some basic estimators

mean; variance: standard deviation; moments; covariance and correlation

27.5 maximum-likelihood method

ml estimator; transformation invariance and bias; efficiency; errors and confidence limits; bayesian interpretation;

large-n behaviour; extended ml method

27.6 the method of least squares

linear least squares; non-linear least squares

27.7 hypothesis testing

simple and composite hypotheses; statistical tests; neyman-pearson; generalised likelihood-ratio; student's t; fisher's f; goodness of fit

27.8 exercises

27.9 hints and answers

28 numerical methods

28.1 algebraic and transcendental equations

rearrangement of the equation; linear interpolation; binary chopping; newton-raphson method

28.2 convergence of iteration schemes

28.3 simultaneous linear equations

gaussian elimination; gauss-seidel iteration; tridiagonal matrices

28.4 numerical integration

trapezium rule; simpson's rule; gaussian integration; monte carlo methods

28.5 finite differences

28.6 differential equations

difference equations; taylor series solutions; prediction and correction; runge-kutta methods; isoclines

28.7 higher-order equations

28.8 partial differential equations

28.9 exercises

28.10 hints and answers

appendix gamma, beta and error functions

a1.1 the gamma function

a1.2 the beta function

a1.3 the error function

index

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精彩短评

- 1、比较喜欢统计那部分，讲的非常精炼，忘记了随时拿出来看看马上就明白了。
- 2、内容丰富，该有的都有了，深入浅出，很难的问题说得很清楚，国内的教材什么时候才能达到这种水平啊，剑桥的东西就是不一样！强烈推荐工科理科的硕士博士们精读。
- 3、此书几乎是把整个大学所需的数学集合在一起，而不是传统的数理方法教材。在这一点上，我还是觉得读专门教材更划算一些。

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