

# 《广义相对论的3+1形式》

## 图书基本信息

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# 《广义相对论的3+1形式》

## 内容概要

尽管物理学家提出了一些新理论，但相对论目前依然是唯一成熟的现代引力理论。而对于相对论的研究也远远没有走到尽头，其丰富内涵依然有待发掘。《广义相对论的3+1形式》讲述了相对论的基本理论和数值方法的基础。对于从事或有志于从事相对论研究的研究人员或研究生，本书都是不可错过的杰作。

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